



# EFFECTS OF MAGNETIC FIELD AND NON-UNIFORM BASIC TEMPERATURE GRADIENT ON THE ONSET OF RAYLEIGH-BENARD CONVECTION IN A FLUID WITH SUSPENDED PARTICLES

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## Abstract

The effects of a non-uniform temperature gradient and magnetic field on the onset of convection in a horizontal layer of Boussinesq fluid with suspended particles confined between an upper free / adiabatic boundary and a lower rigid / isothermal boundary have been considered. A linear stability analysis is performed. The microrotation is assumed to vanish at the boundaries. The Galerkin technique is used to obtain the eigenvalues. The influence of various parameters on the onset of convection has been analysed. Six different non-uniform temperature profiles are considered and their comparative influence on onset is discussed. It is observed that the electrically conducting fluid layer with suspended particles heated from below is more stable compared to the classical electrically conducting fluid without suspended particles. The critical wave number is found to be insensitive to the changes in the parameters but sensitive to the changes in the Chandrasekhar number.

## Introduction

The theory of Rayleigh-Benard instability of a horizontal liquid layer with free upper surface over a heated plate has many important applications in a number of engineering problems, such as in oil extraction from porous medium, energy storage in molten salts, and chemical engineering of paints, colloids and detergents. The instability

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of Rayleigh-Benard convection is due to the effect of the thermal buoyancy. Theoretical studies of the onset of convection in classical viscous fluids with non-uniform heating have been made by Currie [4] with isothermal boundaries and by Nield [12] with adiabatic boundaries and showed that in the case of piecewise linear temperature profile the onset of convection could occur at a smaller Rayleigh number than that of uniform heating. The non-uniform temperature gradient finds its origin in transient heating or cooling at the boundaries and as a result the basic temperature profile depends explicitly on position and time. This has to be determined by solving the coupled momentum and energy equations. This coupling also makes the problem very complicated. In the present study, therefore, we adopt a series of temperature profiles based on a simplification in the form of a quasi-static approximation (Currie [4], Lebon and Cloot [10] and Rudraiah et al [14]) that consists of freezing the temperature distribution at a given instant of time. In this method, we assume that the perturbation grows much faster than the initial state and hence freeze the initial state into some spatial distribution. This hypothesis is sufficient for our purpose because we are interested only in finding the conditions for the onset of convection. Even with these simplifications, the solutions to the variable-coefficients stability equations pose a problem because the temperature gradient varies with depth.

Micropolar fluid theories [6-8] describe some physical systems, which do not satisfy the Navier-Stokes equation. To explain the kinematics of such media two new variables should be added to the velocity. These variables are the spin, responsible for microrotations, and the micro inertia tensor, which accounts for the atoms and molecules inside the macroscopic fluid particles. These fluids are able to describe the behaviour of suspensions, liquid crystals, blood, etc (see Power [14], Lukaszewicz [11] and Eringen [9]). Chandra [2] observed in his experiments that adding smoke particles to a layer of gas could decrease the Rayleigh number at which convective motion commences. Since the particle spin associated with Eringen's theory could possibly be appropriate to the added dust situation described by Chandra [2], there may be dust, dirt, ice or raindrops, or other additives. Thus we believe that the Eringen micropolar convection model may be applicable to geophysical or industrial convection contexts. The Rayleigh-Benard situation in Eringen's micropolar fluids has been investigated by many authors [1,4,13,15-23]. The main result from all these studies is that for heating from below stationary convection is the preferred mode. The effect of non-uniform basic temperature gradients on the onset of Rayleigh-Benard convection in a micropolar fluid has not been given any attention. Hence, the aim of this paper is to study the effect of magnetic field and non-uniform basic temperature gradients on Rayleigh-Benard convection with the object of understanding the control of convection. A single term Galerkin method expansion procedure is used here with the intention of obtaining reasonable results with minimum of mathematics.

## Mathematical Formulation

Consider an infinite horizontal layer of a Boussinesquian, electrically conducting fluid, with non-magnetic suspended particle, of depth 'd' permeated by an externally applied uniform magnetic field normal to the layer (see figure (1)). A Cartesian co-ordinate system is taken with origin in the lower boundary and z-axis vertically upwards. Let  $\Delta T$  be the temperature difference between the upper and lower boundaries. The body forces acting on the fluid are buoyancy and magnetic field. The governing equations for the Rayleigh-Benard situation in a Boussinesquian fluid with suspended particles are:

Continuity Equation

$$\nabla \cdot \bar{q} = 0 \quad (1)$$

Conservation of linear momentum

$$\rho_o \left[ \frac{\partial \bar{q}}{\partial t} + (\bar{q} \cdot \nabla) \bar{q} \right] = -\nabla P - \rho_o g \hat{k} + (2\zeta + \eta) \nabla^2 \bar{q} + \zeta \nabla \times \bar{\omega} + \mu_m (\bar{H} \cdot \nabla) \bar{H}, \quad (2)$$

Conservation of angular momentum

$$\rho_o I \left[ \frac{\partial \bar{\omega}}{\partial t} + (\bar{q} \cdot \nabla) \bar{\omega} \right] = (\lambda' + \eta') \nabla (\nabla \cdot \bar{\omega}) + \eta' \nabla^2 \bar{\omega} + \zeta (\nabla \times \bar{q} - 2\bar{\omega}), \quad (3)$$

Conservation of energy

$$\frac{\partial T}{\partial t} + \left( \bar{q} \cdot \frac{\beta}{\rho_o C_v} \nabla \times \bar{\omega} \right) \cdot \nabla T = \chi \nabla^2 T \quad (4)$$

Equation of State

$$\rho = \rho_o [1 - \alpha (T - T_o)] \quad (5)$$

Magnetic induction equation

$$\frac{\partial \bar{H}}{\partial t} + (\bar{q} \cdot \nabla) \bar{H} = (\bar{H} \cdot \nabla) \bar{q} + \gamma_m \nabla^2 \bar{H} \quad (6)$$

where  $\bar{q}$  is the velocity,  $\bar{\omega}$  is the spin,  $T$  is the temperature,  $\bar{H}$  is the

magnetic field,  $P = p + \frac{\mu_m}{2} H_o^2$  is the hydromagnetic pressure,  $\rho$  is

the density,  $\rho_o$  is the density of the fluid at a reference temperature  $T = T_o$ ,  $g$  is the acceleration due to gravity,  $\zeta$  is the coupling viscosity coefficient or vortex viscosity,  $\eta$  is the shear kinematic viscosity coefficient,  $I$  is the moment of inertia,  $\lambda'$  and  $\eta'$  are the bulk and shear spin viscosity

coefficient,  $\beta$  is the micropolar heat conduction coefficient,  $C_v$  is the specific heat,  $\chi$  is the thermal conductivity,  $\alpha$  is the coefficient of thermal expansion and  $\gamma_m = 1/\mu_m \sigma_m$  is the magnetic viscosity ( $\sigma_m$  : electrical conductivity and  $\mu_m$  : magnetic permeability). All the viscosity coefficients, heat conduction coefficient and thermal conductivity are thermodynamically restricted to be positive quantities on the assumption of Clausius-Duhem inequality (see Eringen [7]). In the energy equation (4) the viscous heating and Joule heating are neglected.

Equations (1)-(6) are solved subject to containment conditions appropriate for a rigid and thermally perfect conducting wall on the underside and by a free surface on the upper side. This free surface is adjacent to a non-conducting medium and subject to a constant heat flux (i.e., adiabatic). Further, the no-spin boundary condition is assumed for microrotation.

### Reference Steady-State

In the reference steady-state the fluid is at rest, the temperature distribution across the layer is non-linear and the lines of force of the magnetic field are vertical. This state is described by :

$$\bar{q}_b = 0, \bar{\omega}_b = 0, \bar{H}_b = H_0 \hat{k}, p = p_b(z), \rho = \rho_b(z), -\frac{d}{dz} \frac{dT_b}{dz} = f(z) \quad (7)$$

The monotonic, non-dimensional basic temperature gradient  $f(z)$  which

is non-negative satisfies the condition  $\int_0^1 f(z) dz = 1$ . The non-

uniformity in  $T_b$  as in (7) finds its origin in transient heating or cooling at the boundaries (Siddheshwar and Pranesh [18,21] and references therein). We have considered various reference steady-state temperature gradients in this paper and these are defined below:

Model	Reference steady-state	$f(x)$
1	Linear	1
2	Heating from below	$\begin{cases} \epsilon^{-1} & 0 \leq z < \epsilon \\ 0 & \epsilon < z \leq 1 \end{cases}$
3	Cooling from above	$\begin{cases} 0 & 0 \leq z < 1-\epsilon \\ \epsilon^{-1} & 1-\epsilon < z \leq 1 \end{cases}$
4	Step function	$\delta(z-\epsilon)$
5	Inverted parabolic	$2(1-z)$
6	Parabolic	$2z$

## Linear Stability Analysis

Let the reference steady-state be disturbed by an infinitesimal perturbation in velocity, microrotation, pressure, temperature and magnetic field. We now have

$$\begin{aligned}\bar{q} &= \bar{q}_b + \bar{q}', & \bar{\omega} &= \bar{\omega}_b + \bar{\omega}', & P &= P_b + P', & \rho &= \rho_b + \rho', \\ T &= T_b + T', & \bar{H} &= \bar{H}_b + \bar{H}'\end{aligned}\quad (8)$$

The primes indicate the primes indicate that the quantities are infinitesimal perturbations and subscript b indicates the reference steady-state value. In the present problem we assume the principle of exchange of stability to be valid and hence deal with only stationary convection.

Substituting equation (8) into equations (1)-(6), we get the linearised equations governing the infinitesimal perturbations in the form :

$$\nabla \cdot \bar{q}' = 0 \quad (9)$$

$$-\nabla P' - \rho' g \hat{k} + (2\zeta + \eta) \nabla^2 \bar{q}' + \zeta \nabla \times \bar{\omega}' + \mu_m H_0 \frac{\partial H'_z}{\partial z} \hat{k} = 0 \quad (10)$$

$$(\lambda' + \eta') \nabla (\nabla \cdot \bar{\omega}') + \eta' \nabla^2 \bar{\omega}' + \zeta (\nabla \times \bar{q}' - 2\bar{\omega}') = 0 \quad (11)$$

$$-\frac{\Delta T}{d} f(z) \left( W - \frac{\beta}{\rho_0 C_v} \nabla \times \bar{\omega}' \cdot \hat{k} \right) = \chi \nabla^2 T' \quad (12)$$

$$\rho' = -\alpha \rho_0 T' \quad (13)$$

$$H_0 \frac{\partial W}{\partial z} \hat{k} + \gamma_m \nabla^2 \bar{H}' = 0 \quad (14)$$

The perturbation equations (9)-(14) are non-dimensionalised using the following definition:

$$(x^*, y^*, z^*) = \frac{(x, y, z)}{d}, \quad \bar{q}^* = \frac{\bar{q}'}{\chi/d}, \quad \bar{\omega}^* = \frac{\bar{\omega}'}{\chi/d^2}, \quad T^* = \frac{T'}{\Delta T}, \quad \bar{H}^* = \frac{\bar{H}'}{H_0} \quad (15)$$

Using equation (13) in equation (10), operating curl twice on the resulting equation, operating curl on equation (11) and non-dimensionalising the two resulting equations and also equations (12) and (14), we get

$$(1+N_1)\nabla^4 W + N_1\nabla^2\Omega_z + R\left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2}\right) + Q\frac{\text{Pr}}{\text{Pm}}\nabla^2\left(\frac{\partial H_z}{\partial z}\right) = 0 \quad (16)$$

$$N_3\nabla^2\Omega_z - 2N_1\Omega_z - N_1\nabla^2 W = 0 \quad (17)$$

$$\nabla^2 T + W - N_5\Omega_z = 0 \quad (18)$$

$$\nabla^2 H_z + \frac{\text{Pm}}{\text{Pr}}\frac{\partial W}{\partial z} = 0 \quad (19)$$

where the asterisks have been dropped for simplicity and

$$N_1 = \frac{\zeta}{\zeta + \eta} \quad (\text{Coupling Parameter}),$$

$$N_3 = \frac{\eta'}{(\zeta + \eta)d^2} \quad (\text{Couple Stress Parameter}),$$

$$N_5 = \frac{\beta}{\rho_0 C_v d^2} \quad (\text{Micropolar Heat Conduction Parameter}),$$

$$\text{Pr} = \frac{\zeta + \eta}{\chi} \quad (\text{Prandtl Number}),$$

$$\text{Pm} = \frac{\zeta + \eta}{\gamma_m} \quad (\text{Magnetic Prandtl Number}),$$

$$R = \frac{\alpha g \Delta T d^3 \rho_0}{(\zeta + \eta)\chi} \quad (\text{Rayleigh Number}) \text{ and}$$

$$Q = \frac{\mu_m H_0^2 d^2}{(\zeta + \eta)\gamma_m} \quad (\text{Chandrasekhar Number}).$$

The infinitesimal perturbations  $W$ ,  $\Omega$ ,  $T$  and  $H_z$  are assumed to be periodic and hence these permit a normal mode solution in the form

$$[W, \Omega, T, H_z] = [W(z), G(z), T(z), H_z(z)] \exp[i(lx + my)] \quad (20)$$

where 1 and m are horizontal components of the wave number  $\bar{a}$ .

Substituting equation (20) into equations (16)-(19), we get

$$(1 + N_1)(D^2 - a^2)^2 W + N_1(D^2 - a^2)G - Ra^2 T + Q \frac{Pr}{Pm} (D^2 - a^2) D H_z = 0 \quad (21)$$

$$N_1(D^2 - a^2)W - N_3(D^2 - a^2)G + 2N_1 G = 0 \quad (22)$$

$$(D^2 - a^2)T + f(z)(W - N_5 G) = 0 \quad (23)$$

$$(D^2 - a^2)H_z + \frac{Pm}{Pr} DW = 0 \quad (24)$$

where  $D \equiv \frac{d}{dz}$

The sets of ordinary differential equations (21)-(24) are approximations based on physical considerations to the system of partial differential equations (16)-(19). Although the relationship between the solutions of the governing partial differential equations and the corresponding ordinary differential equations has not been established, these linear models reproduce qualitatively the convective phenomena observable through the full system.

Eliminating  $H_z$  between equations (21) and (24), we get

$$(1 + N_1)(D^2 - a^2)^2 W + N_1(D^2 - a^2)G - Ra^2 T - QD^2 W = 0. \quad (25)$$

Equations (22), (23) and (25) are solved subject to the following boundary conditions:

$$\begin{aligned} W = DW = T = G = 0 & \quad \text{at } z = 0, \\ W = D^2 W = DT = G = 0 & \quad \text{at } z = 1, \end{aligned} \quad (26)$$

Equation (26) indicates the use of rigid, isothermal lower boundary and upper, free, thermally insulating boundary (with respect to the perturbation). The condition on G is the spin-vanishing boundary condition.

We now use the single-term Galerkin method to find the critical eigenvalue to equations (22), (23) and (25) that gives general results on the eigen value of the problem for various basic temperature gradients using simple, polynomial, trial functions for the lowest eigen value. We obtain an approximate solution of the differential equations with the given boundary conditions by choosing trial functions for velocity, microrotation and

temperature perturbations that may satisfy some of the boundary conditions but may not exactly satisfy the differential equations. This leads to residuals when the trial functions are substituted into the differential equations. The Galerkin method requires the residual to be orthogonal to each individual trial function.

In the Galerkin procedure, we expand the velocity, microrotation and temperature by,

$$W(z,t) = \sum A_j(t) W_j(z), \quad G(z,t) = \sum B_j(t) G_j(z), \quad T(z,t) = \sum C_j(t) T_j(z)$$

where  $W_j(z)$ ,  $G_j(z)$  and  $T_j(z)$  are polynomials in  $z$  that generally have to satisfy the given boundary conditions. For the single term Galerkin expansion technique we take  $i=j=1$ .

Multiplying equation (25) by  $W$ , equation (22) by  $G$  and equation (23) by  $T$ , integrating the resulting equation by parts with respect to  $z$  from 0 to 1 and taking  $W = AW_1$ ,  $G = BG_1$  and  $T = CT_1$ , in which  $A$ ,  $B$  and  $C$  are constants and  $W_1$ ,  $G_1$  and  $T_1$  are trial functions. This procedure yields the following equation for the Rayleigh number  $R$ :

$$R = \frac{\langle T_1 (D^2 - a^2) T_1 \rangle [C_1 C_2 + N_1^2 C_3]}{a^2 \langle W_1 T_1 \rangle C_4} \quad (27)$$

where

$$\begin{aligned} C_1 &= N_3 \langle G_1 (D^2 - a^2) G_1 \rangle - 2N_1 \langle G_1^2 \rangle, \\ C_2 &= (1 + N_1) \langle W_1 (D^2 - a^2)^2 W_1 \rangle - Q \langle W_1 D^2 W_1 \rangle, \\ C_3 &= \langle W_1 (D^2 - a^2) G_1 \rangle \langle G_1 (D^2 - a^2) W_1 \rangle, \\ C_4 &= N_1 N_5 \langle f(z) G_1 T_1 \rangle \langle G_1 (D^2 - a^2) W_1 \rangle - \langle f(z) W_1 T_1 \rangle C_1. \end{aligned}$$

In equation (27),  $\langle - - \rangle$  denotes integration with respect to  $z$  between  $z = 0$  and  $z = 1$ . We note here that  $R$  in equation (27) is a functional and the Euler-Lagrange equations for the extremisation of  $R$  are equations (22), (23) and (25).

The trial functions satisfying (26) are

$$W_1 = 2z^4 - 5z^3 + 3z^2, \quad T_1 = z(z-2), \quad G_1 = z(1-z). \quad (28)$$



Substituting (28) in equation (27) and performing the integration, we get

$$R = \frac{(5 + 2a^2)}{36} \left\{ \frac{28 y_1 [(1 + N_1) y_2 + 216Q] - N_1^2 y_3^2}{N_1 N_3 y_3 \langle f(z) T_1 G_1 \rangle - 28 y_1 \langle f(z) W_1 T_1 \rangle} \right\} \quad (29)$$

where

$$y_1 = N_3 (10 + a^2) + 2N_1, \quad y_2 = 4536 + 432a^2 + 19a^4, \quad y_3 = 126 + 13a^2.$$

For a given  $f(z)$ ,  $R$  attains its minimum value  $R_c$  at  $a = a_c$ .

The integrals  $\langle f(z) W_1 T_1 \rangle$  and  $\langle f(z) T_1 G_1 \rangle$  will have the following forms depending on the nature of basic temperature profile.

Model 1. Linear temperature profile

$$\langle f(z) W_1 T_1 \rangle = \frac{-2}{35}, \quad \langle f(z) T_1 G_1 \rangle = \frac{-7}{60}$$

Model 2. Piecewise linear heating from below temperatures profile

$$\langle f(z) W_1 T_1 \rangle = \frac{1}{280} (40\epsilon^6 - 210\epsilon^5 + 364\epsilon^4 - 210\epsilon^3),$$

$$\langle f(z) T_1 G_1 \rangle = \frac{1}{60} (-12\epsilon^4 + 45\epsilon^3 - 40\epsilon^2).$$

Model 3. Piecewise linear cooling from above temperature profile

$$\langle f(z) W_1 T_1 \rangle = \frac{1}{280} (40\epsilon^6 - 70\epsilon^5 - 56\epsilon^4 + 140\epsilon^3 - 70\epsilon^2),$$

$$\langle f(z) T_1 G_1 \rangle = \frac{1}{60} (-12\epsilon^4 + 15\epsilon^3 - 20\epsilon^2 - 30\epsilon).$$

Model 4. Step function temperature profile

$$\langle f(z) W_1 T_1 \rangle = \epsilon^6 - \frac{9}{2}\epsilon^5 + \frac{13}{2}\epsilon^4 - 3\epsilon^3, \quad \langle f(z) T_1 G_1 \rangle = -\epsilon^4 + 3\epsilon^3 - 2\epsilon^2.$$

Model 5. Inverted temperature profile

$$\langle f(z) W_1 T_1 \rangle = \frac{-19}{420}, \quad \langle f(z) T_1 G_1 \rangle = \frac{-1}{10}$$

Model 6. Parabolic temperature profile

$$\langle f(z) W_1 T_1 \rangle = \frac{-29}{420}, \quad \langle f(z) T_1 G_1 \rangle = \frac{-2}{15}$$

## Result and Discussion

In the paper we study the effects of non-uniform basic temperature gradient and magnetic field on the onset of Rayleigh-Benard convection in an electrically conducting micropolar fluid. Six non-uniform temperature profiles are chosen for study. It is observed that for the critical Rayleigh number,  $R_c$ , the following inequality holds for the six models under question

$$R_{c4} < R_{c3} < R_{c2} < R_{c6} < R_{c1} < R_{c5},$$

i.e., the step function is the most destabilising basic temperature distribution and inverted parabolic is the most stabilising basic temperature distribution. In the case of piecewise linear and step function profiles, the critical Marangoni number  $R_c$  depends on the thermal depth,  $\varepsilon$ , in addition to depending on the parameters of the problem. In the case of piecewise linear profile heating from below, cooling from above and step function profiles the minimum value of  $R_c$  is attained at  $\varepsilon = 0.86$ ,  $\varepsilon = 0.55$  and  $\varepsilon = 0.64$  respectively.

Before embarking on a discussion of the results let us make some comments on the parameters  $N_1$ ,  $N_3$  and  $N_5$  arising due to the suspended particles. Assuming the Clausius - Duhem inequality Eringen[8] presented certain thermodynamic restrictions, which lead to non-negativeness of  $N_1$ ,  $N_3$  and  $N_5$ . For  $\zeta = 0$  ( $N_1 = 0$ ) it is clear that equation (21) for  $W$  becomes independent of  $G$ , i.e. it is uncoupled. As  $\zeta \rightarrow \infty$ , we see that  $N_1 \rightarrow 1$  and  $N_3 \rightarrow 0$ . This is the Stokesian description of suspension. Thus, it is obvious that couple stress comes into play only at small values of  $N_3$ . This support the contention that  $N_1 \in [0, 1]$  and  $N_3$  is small positive real number. Coming to  $N_5$  it has to be finite because the increasing of concentration has to practically stop somewhat and hence  $N_5$  has to be a positive, finite real number. With the above background and with the motive specified in the introduction we now discuss the results presented by the figures (1).

Figure - 1

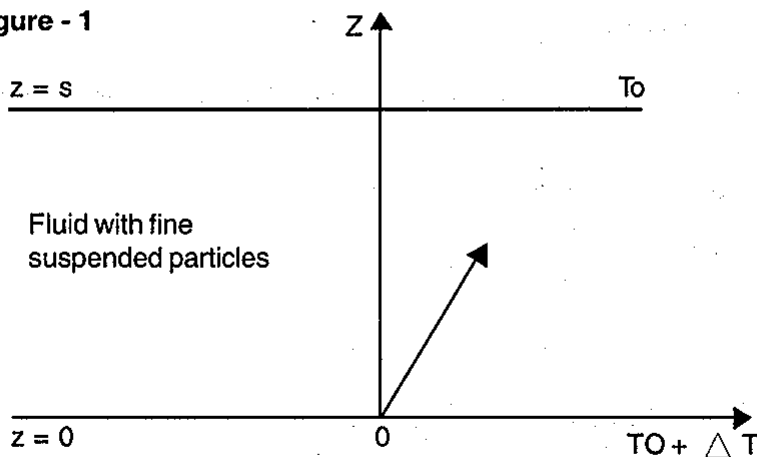


Figure (2 a) is the plot of  $R_c$  versus the coupling parameter  $N_1$  for different non-uniform temperature gradients and Chandrasekhar number  $Q$ . Clearly  $R_c$  increase with  $N_1$ . Increase in  $N_1$  indicates the increase in the concentration of microelements. These elements consume the greater part of the energy of the system in developing the gyration velocities of the fluid and as a result the onset of convection is delayed. Therefore, the increase in  $N_1$  is to stabilise the system.

Figure (2 b) is the plot of  $R_c$  versus the couple stress parameter  $N_3$  for different non-uniform temperature profiles and  $Q$ . Clearly  $R_c$  decreases with the increase in  $N_3$  and ultimately levels off to the Newtonian value. Increase in  $N_3$ , decreases the couple stress of the fluid which causes a decrease in microrotation and hence makes the system more unstable.

Figure (2 c) is the plot of  $M_c$  versus the micropolar heat conduction parameter  $N_5$  for different non-uniform temperature profiles and  $Q$ . When  $N_5$  increases, the heat induced into the fluid due to these microelements also increases, thus reducing the heat transfer from bottom to top. The decrease in heat transfer is responsible for delaying the onset of instability. This result can also be anticipated because Eq. (4) clearly shows that the effect of the suspended particles is to deduct from the velocity. Thus increase in  $N_5$  is to stabilise the system.

The effects of  $N_1$ ,  $N_3$  and  $N_5$  on  $R_c$  is true both in the presence and absence of a magnetic field. When the strength of the magnetic field increases, the system becomes stable, a result which is as seen in the case of classical fluid. On the other hand, when the microrotation and the magnetic field are simultaneously present, the stabilizing effect of  $N_1$  is reduced, being counteracted by the magnetic field. Chandrasekhar [3] has noticed the similar phenomenon, when the system is subject to both rotation and magnetic field. The above phenomenon can be physically explained as follows:

When the magnetic field strength permeating the medium is considerably strong, it induces viscosity into the fluid, and the magnetic lines are distorted by convection. Then these magnetic lines hinder the growth of disturbances, leading to the delay in the onset of instability. However, the viscosity produced by the magnetic field lessens the rotation of the fluid particles, thus controlling the stabilizing effect of  $N_1$ .

From the calculations it has also been found that the critical wave number is, in general, insensitive to the changes in the micropolar parameters but is influenced by the magnetic field. A strong magnetic field succeeds in inducing only the coupling number  $N_1$  into influencing  $a_c^2$ .

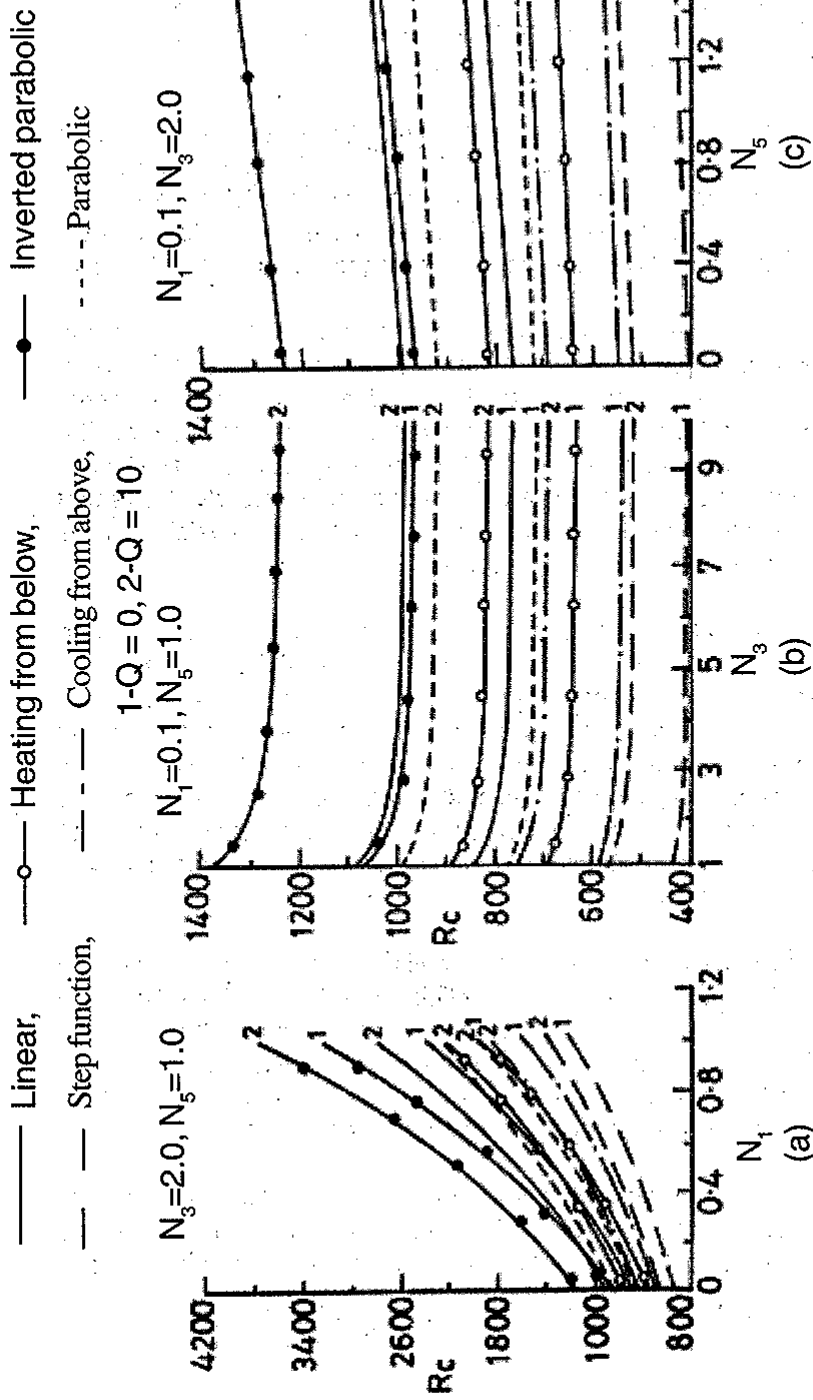


FIG. 2. PLOT OF  $R_c$  VS. (a)  $N_1$ , (b)  $N_3$  AND (c)  $N_5$  WITH RESPECT TO LOWER RIGID ISOTHERMAL AND UPPER FREE ADIABATIC FOR DIFFERENT VALUES OF  $Q$  AND DIFFERENT NON-UNIFORM BASIC TEMPERATURE GRADIENTS

The above results indicate that the externally applied magnetic field is an effective means of controlling Rayleigh – Benard convection in electrically conducting micropolar fluids. The results suggest that Rayleigh – Benard convection in Newtonian fluids may be delayed by adding micron sized electrically inert suspended particles. Further, by creating conditions for an appropriate basic temperature gradient we can also make an a priori decision on advancing or delaying convection.

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